

Collective subscriptions: a novel funding tool for crowdsourced network infrastructures

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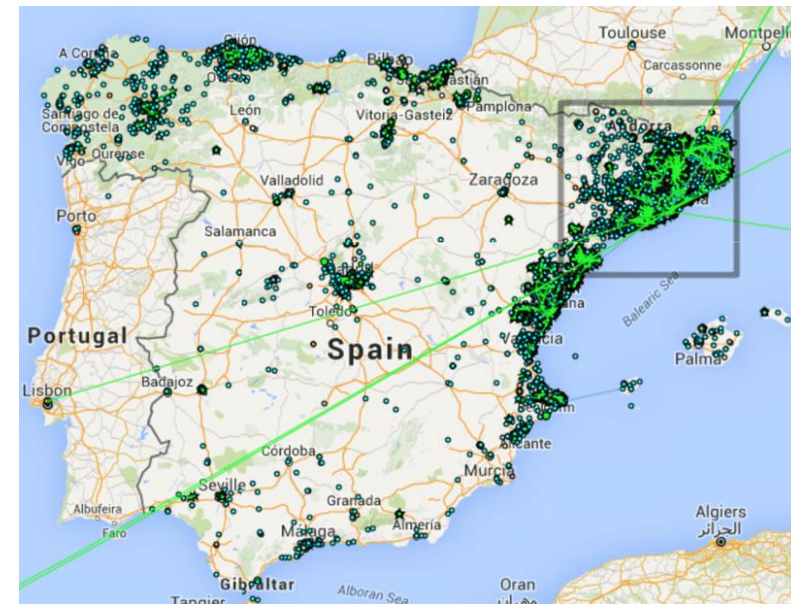
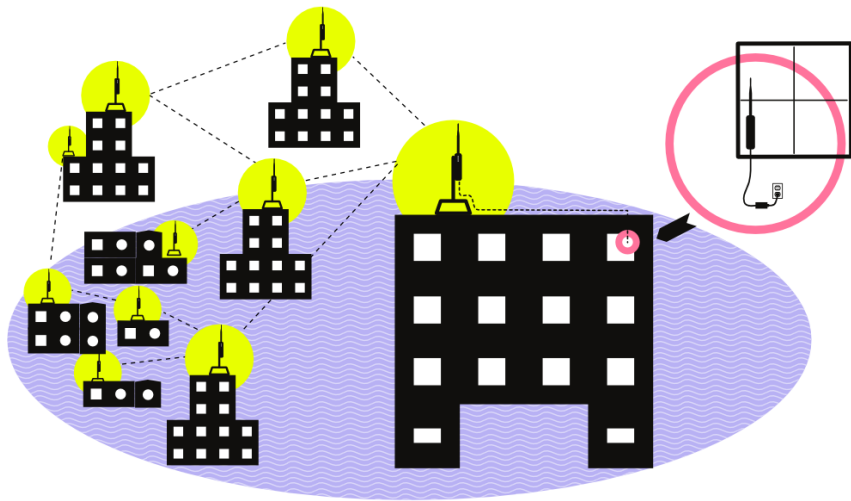
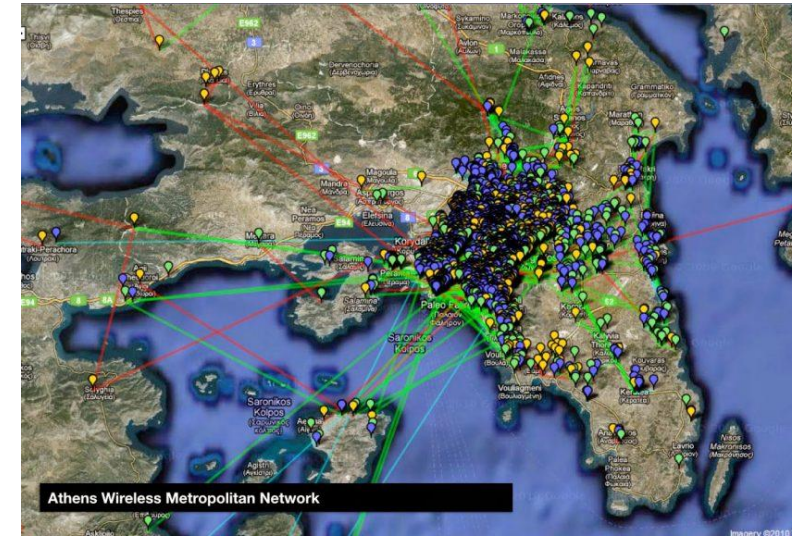


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Community Networks worldwide : a 20-year long story

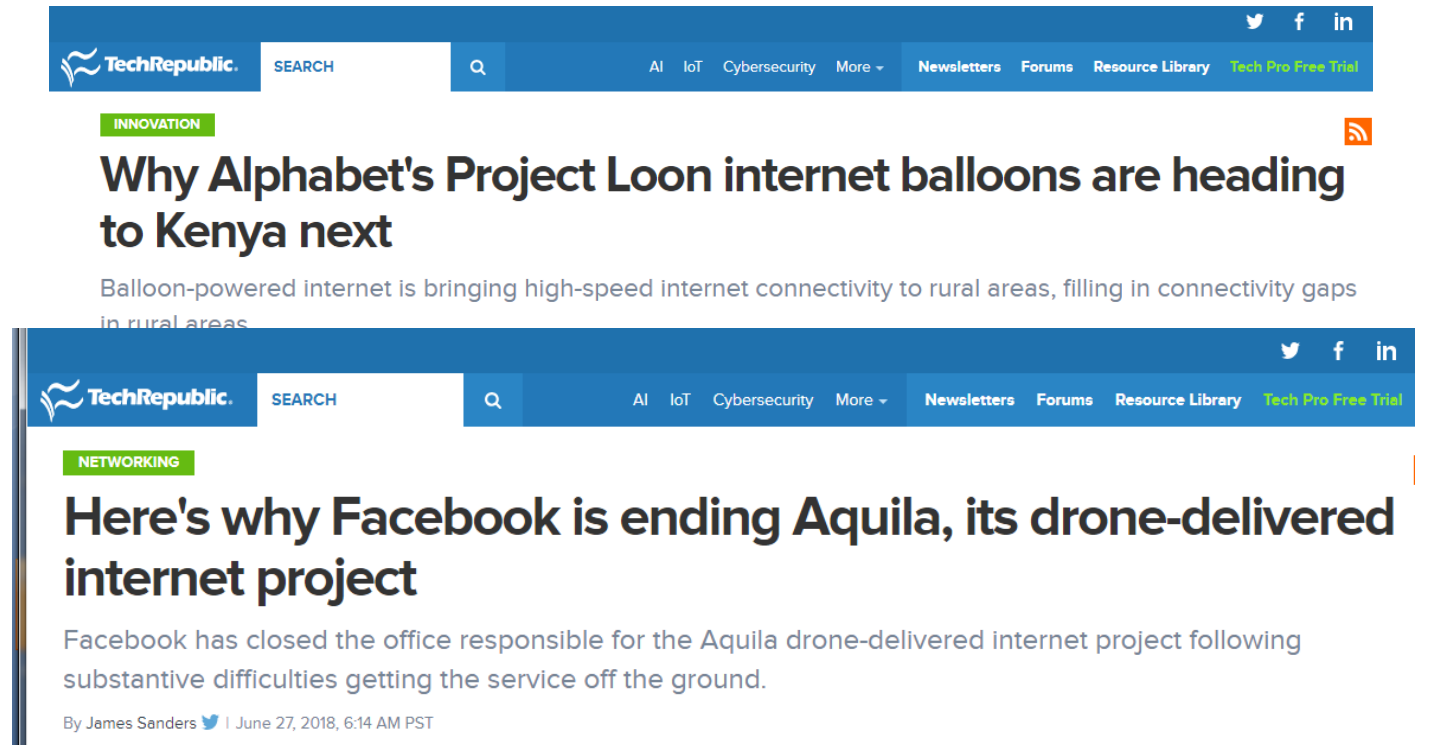
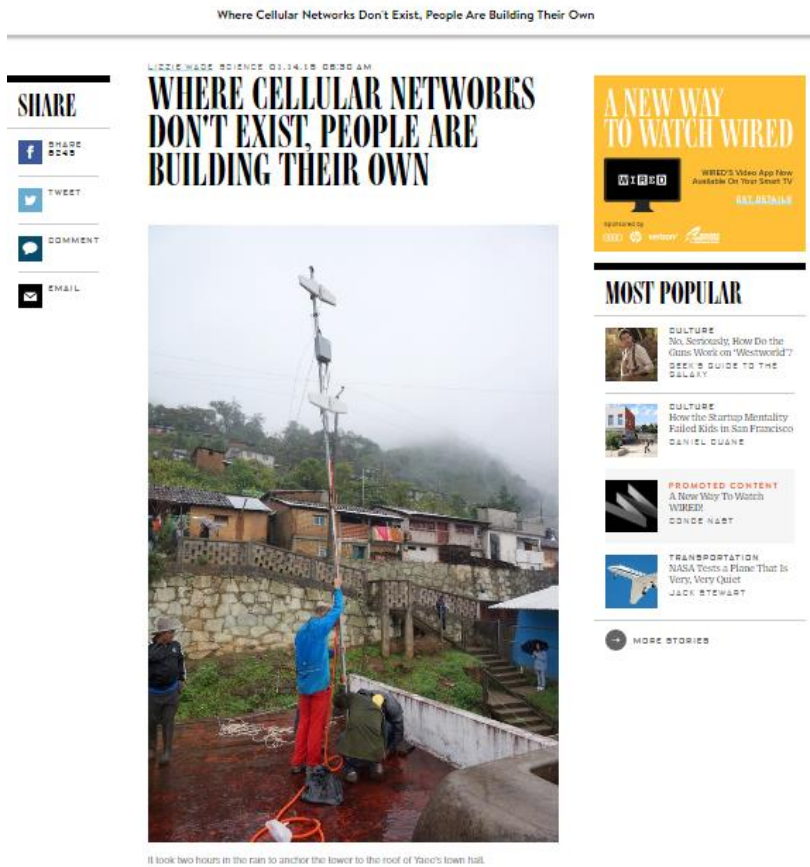
- grassroots initiatives in both urban and rural areas
- addressing a broad mix of needs
 - experimentation with technology and DIY, digital divide, autonomy and community ideals



Three good reasons for renewed interest in CNs

1. Bridging the digital divide- connecting the next billion of people

- the “local” bottom-up approach to the problem
- ...as opposed to ambitious global top-down approaches to the problem



Three good reasons for renewed interest in CNs

2. Enabling broadband connectivity agendas: CNs as network infrastructure providers

- e.g., Broadband Europe 2020 and 2025 or 5G mobile systems



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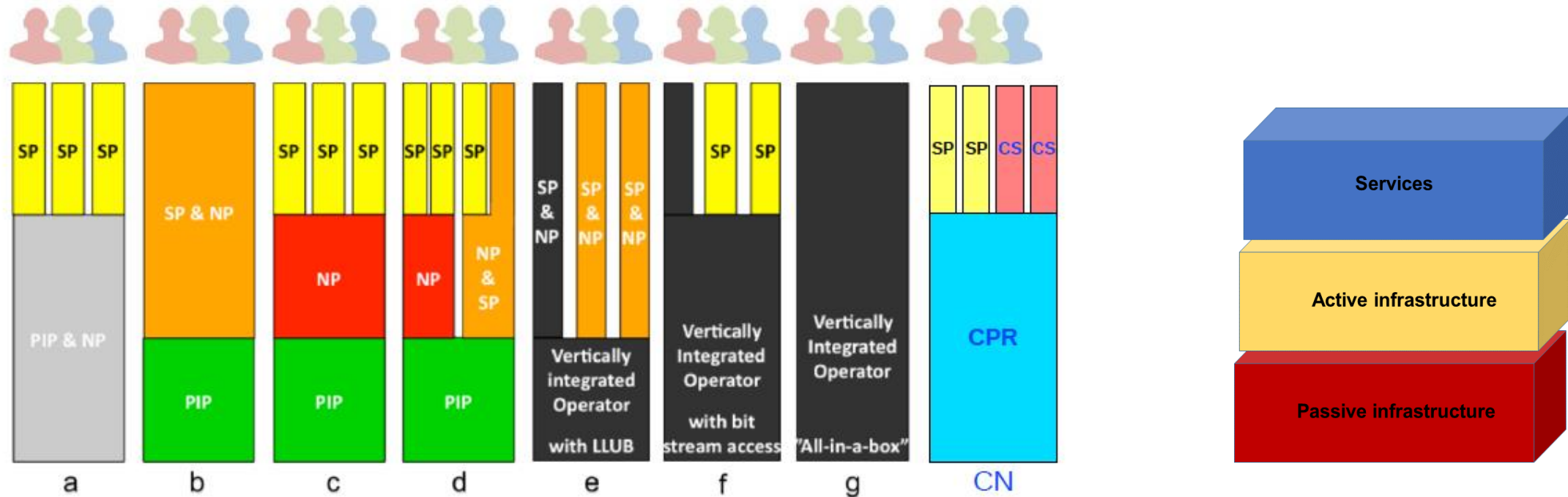
European Commission

Guide to High-Speed Broadband Investment

Three good reasons for renewed interest in CNs

3. Democratizing the market

- through fostering more open telecom network models against dominant trends for verticals



Economic sustainability of CNs

CN expenses

Capital expenses (CapEx)

- Equipment: access points, routers, antennas, servers
- Installation costs
 - Mounting antennas and access points
 - Digging costs (when deploying fiber)

Operational expenses (OpEx)

- Cost of peering agreements for Internet access (leased lines)
- Maintenance of network nodes
- Software for network management, network monitoring, billing
- Electricity costs

CN revenue sources

- Donations from supporters
 - crowd-funding, regular or one-time donations, investments in the infrastructure
- Support from public agencies and institutions
 - public funds from municipalities or local authorities, grants from non-profit institutions
- Funding from private sector
 - synergies with commercial for-profit service providers under commons-based policies
- Member subscriptions
 - monthly or yearly
 - All CN success stories rely on their members' subscriptions

Individual subscriptions and free riding

The de-facto subscription scheme is fixed-price subscriptions. The subscription fee

- on the one hand, should maximize inclusion of the community
- on the other hand, should secure sufficient revenue for the CN economic sustainability

Not always an easy task:

- **free riding** is frequent in these CNs, not least due to affordability



Toy example : 5 users who can afford *15, 13, 12, 8, 5 Euros per month*, respectively, for a subscription.

If the subscription fee f_s is set to:

$f_s \leq 5$, all five users can join, paying up to 5 each → CN revenue up to 25 Euros

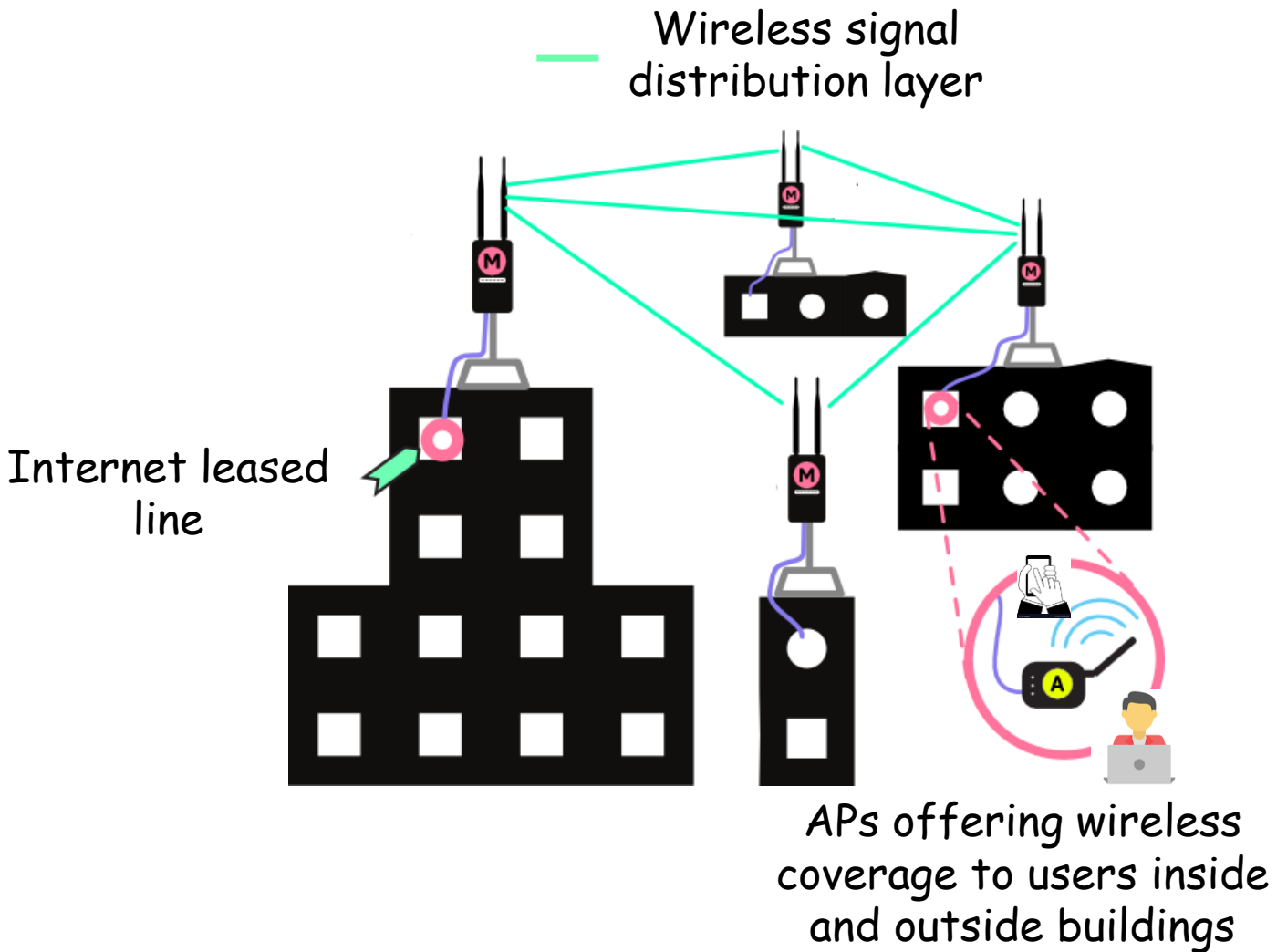
$5 < f_s \leq 8$, the first four users can join, paying up to 8 each → CN revenue up to 32 Euros

$8 < f_s \leq 12$, the first three users can join, paying up to 12 each → CN revenue up to 36 Euros

Collective subscriptions - outline

- **Idea** : instead of charging individual CN users, charge the CN node owners *only* and share the subscription costs with users subscribing to the node
 - attempt to accommodate the varying amounts users are willing to pay for membership and connectivity
- **Outline of the remainder of the presentation**
 - the collective subscriptions optimization problem
 - system model, assumptions, problem formulation, characterization in the general case
 - solution of the problem
 - structural properties, enumerative algorithm over a reduced search space
 - evaluation of the scheme
 - performance characteristics, comparison with fixed-price individual subscriptions

System model - actors



Set of users, U

- assess differently the Internet connectivity value \rightarrow individual **price ceilings** $r_j, j \in U$
- each user u prefers to join the subscription of a certain set of CN nodes N_u out of the full CN node set N
 - e.g., those she uses most frequently, close to her house or neighborhood

CN operator, CNO

- sets the node subscription fee f_s and distributes users to node subscriptions
- seeks to maximize revenue but also let as many as possible join the CN

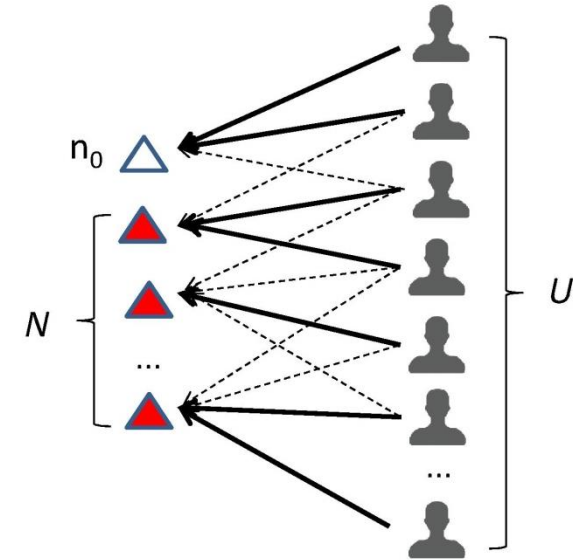
Collective subscriptions: three assumptions/properties

- No discrimination at node subscription level ASS1
 - the fee f_s charged by the CNO is common for all CN nodes
- No discrimination at user level *within a given node* ASS2
 - if k users join a node subscription, the fee share each one pays is f_s/k
 - however, users assigned to different nodes may end up paying different amounts
 - the more users join a CN node subscription, the less the fee share for each user (positive externality)
 - ⇒ an incentive for CN node owners to recruit more users
- The CNO is aware of the true price ceilings of users ASS3
 - the strongest assumption (and the main subject of current follow-up work)

Optimizing collective subscriptions

Let $P = (p_0, p_1, p_2, \dots, p_N)$ be a partition of CN users to the N nodes

- $k_n = |p_n|$, the number of users joining the subscription of node n
- p_0 : set of users who do not join the CN (they cannot afford the fee)
- α : an upper bound on the number of users who cannot afford the subscription



Then:

- The maximum fee the CNO can collect out of node n is : $fee(n) = k_n \min_{u \in p_n} r_u$
- The total fee that the CNO can collect out of the CN is : $R_{CNO}(p) = \min_{\substack{n \in N \\ k_n > 0}} fee(n) \cdot \sum_{n \in N} 1_{k_n > 0}$

- The objective of CNO is to $\max_p R_{CNO}(p)$ (OPT)

$$s. t. \quad k_n = \sum_{u: n \in N_u} x_{un} \quad \forall n \in N \cup n_0$$

$$\sum_{n \in N_u \cup n_0} x_{un} = 1 \quad \forall u \in U \quad \text{assignment constraints}$$

$$k_0 \leq \alpha \quad \text{inclusion constraint}$$

$$x_{un} \in \{0,1\} \quad u \in U, n \in N \cup n_0$$

Problem characterization

The problem (OPT) is NP-hard in the general case

- non-identical user price ceilings
- non-identical user subscription preferences (distinct sets N_u)

The problem simplifies under special cases

- identical user price ceilings ($r_u = r_v = r \quad \forall u, v \in U$)
 - the problem reduces to a special case of the restricted max-min fair allocation problem
- identical user price ceilings **and** subscription preferences ($N_u = N$)
 - trivial solution to the assignment problem
- identical user subscription preferences ($N_u = N$), equivalently: user indifference to the subscription assignment
 - ...see the remainder

Collective subscriptions : identical user subscription preferences

Idea : enumerate possible solutions albeit in a significantly reduced search space

Definition : r – ordered partition $p_{ord}(k_0, k_1, k_2, \dots, k_N)$ with $k_j \geq k_{j+1}$, $j \in [1..N-1]$

The single partition p (of users to node subscriptions) out the set of all partitions $P(p_0, p_1, p_2, \dots, p_N)$ such that

- $|p_j| = k_j$, $j \in [1..N]$
- $\max_{u \in p_j} r_u \leq \min_{u \in p_{j+1}} r_u$, $j \in [1..N-1]$

Example: $N = 4$, $U = 13$, $\bar{r} = [2, 3, 3, 5, 6, 7, 8, 10, 12, 14, 15, 15, 16]$

Then:

$$p_{ord}(1, 4, 3, 3, 2) = \{\{2\}, \{3, 3, 5, 6\}, \{7, 8, 10\}, \{12, 14, 15\}, \{15, 16\}\}$$

$$p_{ord}(1, 5, 4, 2, 1) = \{\{2\}, \{3, 3, 5, 6, 7\}, \{8, 10, 12, 14\}, \{15, 15\}, \{16\}\}$$

$$p_{ord}(0, 5, 4, 2, 2) = \{\emptyset, \{2, 3, 3, 5, 6\}, \{7, 8, 10, 12\}, \{14, 15\}, \{15, 16\}\}$$

Collective subscriptions : identical user subscription preferences

Proposition : Any partition $p(k_0, \sigma(k_1), \sigma(k_2), \dots, \sigma(k_N))$, where σ is an arbitrary permutation of the set $\{k_1, k_2, \dots, k_N\}$, can be converted to an r – ordered partition $p_{ord}(k_0, k_1, k_2, \dots, k_N)$ so that

$$R_{CNO}(p) \leq R_{CNO}(p_{ord})$$

Example:

arbitrary partition (1,4,3,3,2)

p_0	p_1	p_2	p_3	p_4
3	5	6	15	2
	15	7	12	10
	8	16	3	
	14			

$$R_{CNO} = 12$$

Algorithm 1 Transformation of an arbitrary partition to its r -ordered counterpart

Input: Partition subset p_0 and subsets p_1, \dots, p_N , indexed in order of decreasing cardinality

Output: Subsets p_0, p_1, \dots, p_N of the r -ordered partition

- 1: **for** every subset $j \in [0..N - 1]$ **do**
 - 2: $z = \max$ value in subset j , $w = \min$ value over subsets indexed in $[j+1..N-1]$, $m =$ subset hosting w
 - 3: **while** $w < z$ **do**
 - 4: move z to the subset m and w to p_j
 - 5: $z = \max$ value in subset j , $w = \min$ value in subsets indexed in $[j+1..N-1]$, $m =$ subset hosting w
 - 6: **end while**
 - 7: **end for**
-

r -ordered partition (1,4,3,3,2)

p_0	p_1	p_2	p_3	p_4
2	5	10	15	16
	3	7	12	15
	6	8	14	
	3			

$$R_{CNO} = 48$$

Collective subscriptions : identical user subscription preferences

Corollary: To find the the optimal partitions of end users to CN node subscriptions, it suffices to search through the set of r – ordered partitions featuring $k_0 \leq a$

- search complexity becomes polynomial $O(N^U)$ instead of exponential $O(U^N)$ to the number of users (note that typically $U \gg N$)

Evaluation of the scheme

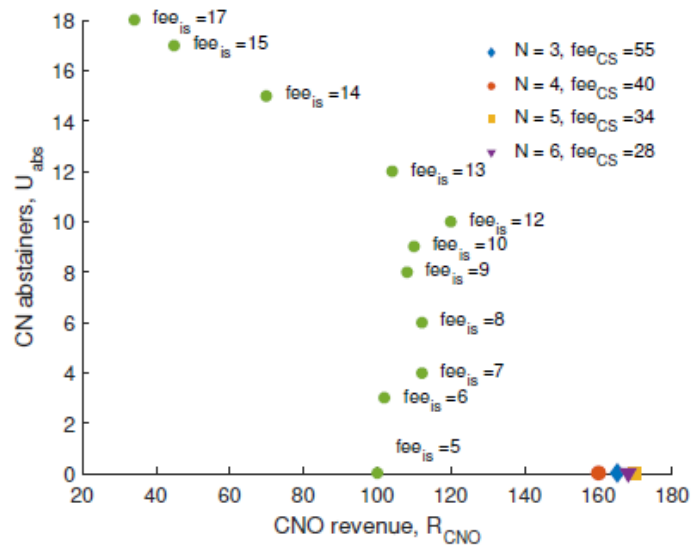
Main questions

- How well can collective subscriptions trade off community inclusion (number of abstainers, U_{abs}) with achievable revenue (R_{CNO})?
 - How do they compare in this with fixed individual subscriptions?
- What other variants of the scheme are possible?

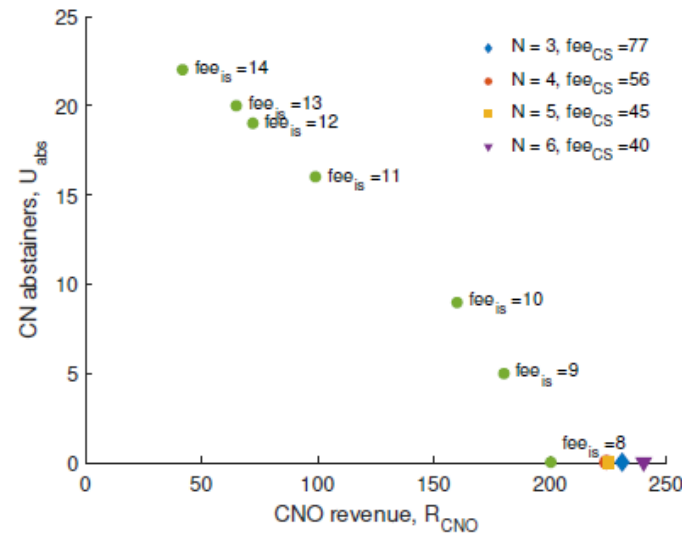
Methodology

- Get (N,U) pairs from real data (drawn from a Greek rural CN) or generate synthetic data
- Synthetic distributions for price ceilings, $r_u \in \{r_{min} \dots r_{max}\}$

Collective vs. individual fixed price subscriptions



$$U = 20, r \sim U\{5, 17\}$$



$$U = 25, r \sim U\{8, 12\}$$

⚙️ Solve OPT with $\alpha = 0$ (include everyone in the CN)

🔍 Collective subscriptions consistently achieve higher revenue than individual subscriptions

- even if users with low price ceilings are excluded from the CN
- CNO revenue gains range from 12.5% to 43% across experiments

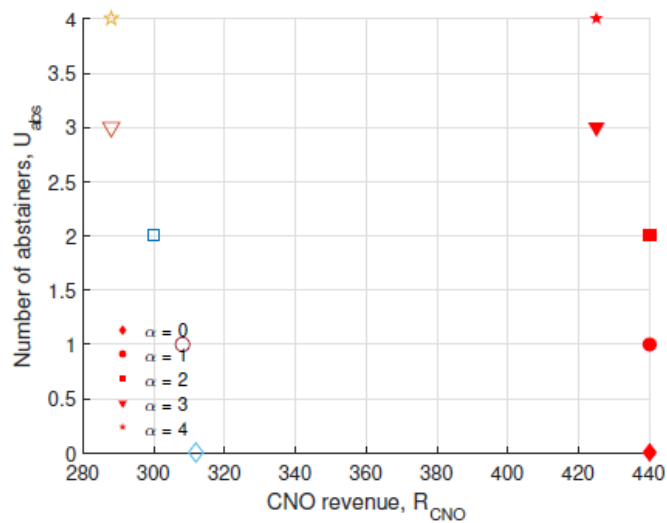
Does this experimental evidence generalize?

Proposition : For any given set of users and their corresponding price ceilings, collective subscriptions yield (R_{CNO}, U_{abs}) values that Pareto – dominate those obtained under fixed price individual subscriptions

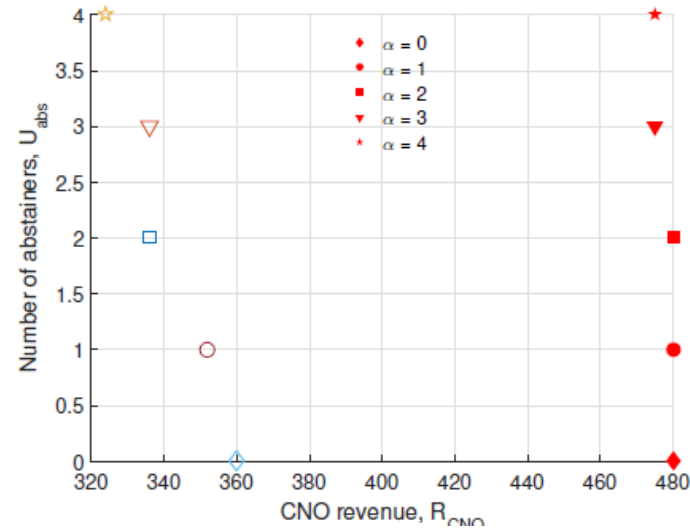
- upon the condition that $U - U_{abs} = \delta \cdot N, \delta \in \mathbb{Z}^+$
- there are (rare, quite extreme cases) that proposition does not hold, i.e., when U is prime and $r_u = r_v \forall u, v \in U$

Revenue vs. community inclusion under collective subscriptions

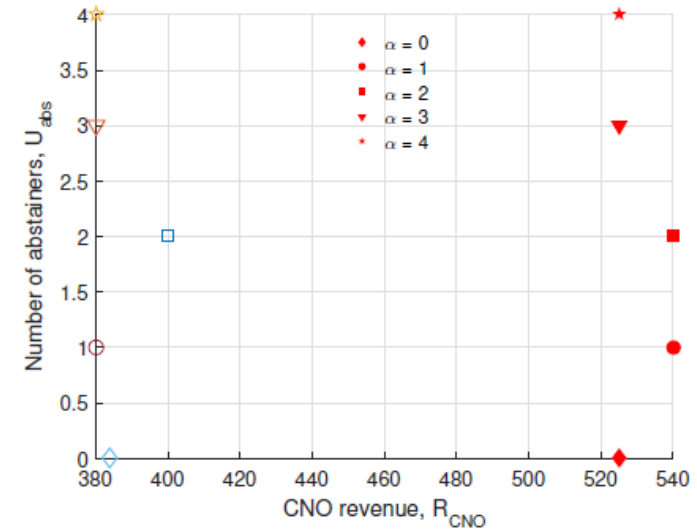
Filled markers correspond to $(U = 40, N = 5)$. Empty ones correspond to $(U = 30, N = 4)$.



$r \sim \{8, 14\}$ for 80% of users



$r \sim U\{8, 20\}$



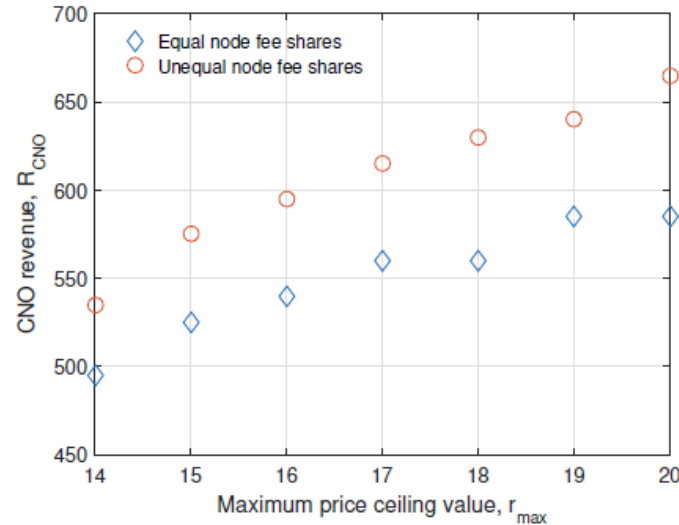
$r \sim \{8, 14\}$ for 20% of users

- ⚙️ Solve (OPT) with the inclusion constraint turned to equality ($k_0 = a$)
- 🔍 For uniform (middle plot) and positively skewed distributions (left plot) of user price ceilings revenue and participation are simultaneously maximized
- 🔍 Under negative skew, the revenue may increase when excluding a few users with the lowest price ceilings

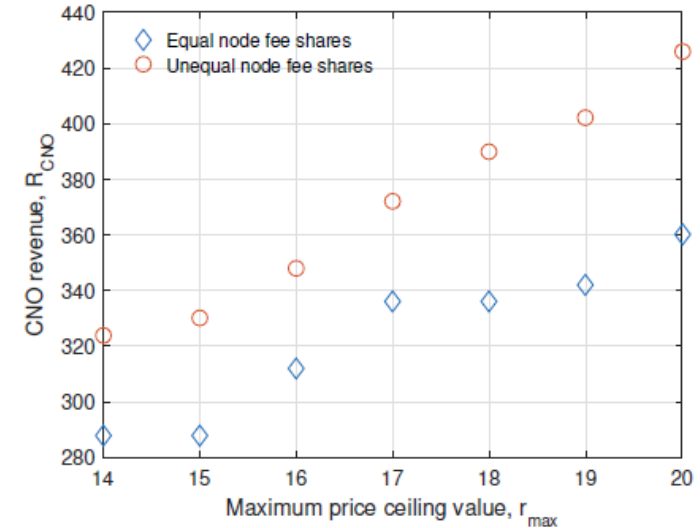
Collective subscriptions with unequal node subscription fee shares



$$U = 40, N = 5, r_{\min} = 5$$



$$U = 50, N = 5, r_{\min} = 8$$



$$U = 30, N = 6, r_{\min} = 8$$

⚙️ Solve a modification of OPT with $fee(n) = \sum_{u \in p_n} r_u$ and $a = 0 \rightarrow$ multi-way partitioning problem

📄 The revenue is consistently higher when the node subscription fee sharing becomes more flexible

- gains in the order of 10% to 25%
- on the downside, the introduced discrimination among users who share the subscription of the same node strengthens the motivation to misreport the price ceilings

Concluding and the way forward

- We have proposed an innovative subscription mechanism for community networks to self-fund their activities and took some steps in analyzing it
 - the mechanism matches well the strong sharing ideals of these crowdsourced infrastructures
- The mechanism demonstrates a clear performance advantage over fixed-price individual subscriptions
 - resulting in higher revenue for the CNO and better inclusion of the end users
 - serves as incentive for recruiting more members to the CN and sharing the subscription cost
- The strongest assumption that has to be relaxed is that end users declare truthfully what they are willing to pay for Internet access
 - users are tempted to underbid in the expectation that they will end up with lower cost shares, possibly at the expense of other users
 - we currently explore how to shape collective subscriptions into a mechanism that induces truthfulness as an equilibrium

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